Academic Year: 2016 – 2017

Semester: Autumn

Date: December 27, 2016



Final Exam

Mathematics: OCM 103

Duration Time: 2 Hours

No. of questions: 4 Total Mark: 60

### **Answer All Questions**

#### **Question 1**

(a)If 
$$A = \begin{bmatrix} 1 & 0 & -2 \\ 2 & 4 & -1 \end{bmatrix}$$
,  $B = \begin{bmatrix} 2 & 0 & 2 \\ 1 & 3 & 1 \end{bmatrix}$  and  $C = \begin{bmatrix} 0 & 3 \\ 2 & 1 \end{bmatrix}$ 

Find, if possible, A + B, A + C,  $A \cdot B$ ,  $C \cdot A$ , |A|, |C|,  $|A^t \cdot B|$ .

(b) Find the eigenvalues and eigenvectors of :  $A = \begin{bmatrix} 2 & 1 \\ 2 & 3 \end{bmatrix}$ .

# **Question 2**

(a) Solve the linear system : x - y + z = 2, x + 2z = 3, 2x - 2y + 2z = 5.

(b) If a drug exists in three dosage forms: The first of concentration 1 mg/tablet, The second of concentration 2 mg / tablet, The third of concentration 4 mg /tablet. If the pharmacist wanted to produce 10 tablets of concentration 3 mg / tablet by mixing whole tablets. Find two possible solutions.

## **Ouestion 3**

(a) Find **y**` where:

(i) 
$$y = 2x^4 + 4^x - 4x$$

(ii) 
$$y = 3 + x^3 . \ln x$$

(iii) 
$$y = \cos x \cdot \log x$$

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$$y = 2x^4 + 4^x - 4x$$
 (ii)  $y = 3 + x^3 . \ln x$  (iv)  $y = \frac{2}{3} + \frac{1}{[x + \sin x]^5}$  (v)  $y = \sqrt{x} + \frac{3x}{4} + \frac{2}{x^5}$ 

(v) 
$$y = \sqrt{x} + \frac{3x}{4} + \frac{2}{x^5}$$

$$(vi) y = \frac{1}{x} + \cos^5 x$$

(b) Find the integrals:

(i) 
$$\int (x^4 + \frac{1}{x^4} + \frac{1}{x}) dx$$

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$$\int (x^4 + \frac{1}{x^4} + \frac{1}{x}) dx$$
 (ii)  $\int (\sqrt{x} + \frac{2^{x+1}}{3^x}) dx$ 

$$(iii)\int (\cos x - 2\sin x) dx$$

(iv) 
$$\int (3^x - 2^x)^2 dx$$

$$(v)\int \ln x \, dx$$

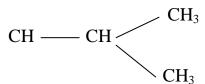
$$(vi) \int \frac{x-1}{x^2 - 2x} \, dx$$

## **Ouestion 4**

(a) If the quantity of a drug in the blood decreases according to the data:

Time:	t	0	2	4	6	8	Hours
Quantity:	у	12	11	9	6	2	Units

From these data, find the relation y = a + bt. Also, find the value of y at t = 3. (b) Write the matrix of the chemical compound :



Good Luck

Dr. Mohamed Eid

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